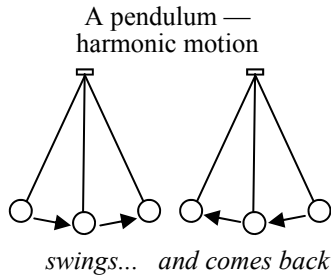
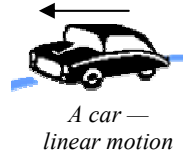


# Harmonic Motion

**Harmonic Motion** is any motion that is repetitive (doing the same thing over and over) and caused by a **restoring force**. Pendulums, bouncing springs, wheels (circular motion), waves, music: these are all harmonic motion.



**Linear motion** goes from here to there: one direction.



*Linear motion—up uses a different force than down*

A bird flying *looks* like harmonic motion because the wings are going up and down. Actually, it is linear motion because up and down require two different sets of muscles.

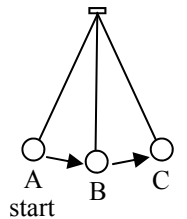
**Restoring force:** a force that tries to return an object to equilibrium (center resting position). If a pendulum is disturbed (moved), gravity (restoring force) pulls it back to center. Because it has too much momentum, it goes past center and keeps going back and forth.

## Parts of Harmonic Motion

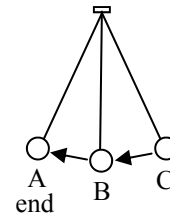
**Cycle:** the repeated portion of the motion; includes all of the steps of the motion.

**Period:** length of time for one cycle; how long it takes for one repetition.

**Frequency:** number of cycles per second in hertz (Hz). A hertz is a cycle per second.



*From A to C is only half a cycle.*



*When the pendulum gets back to A it has completed one cycle and starts over.*

*If it takes 2 seconds for the pendulum to go from A to C and back to A, the pendulum's period is 2 seconds.*

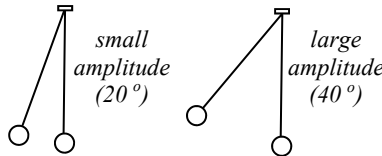
Period (in secs) →  $T = \frac{1}{f}$  OR  $f = \frac{1}{T}$  ← Period (in secs)

← Frequency (in hertz)

Ex: A pendulum has a frequency of 4 Hz. Find its period.	
$f = 4 \text{ Hz}$ $T = ?$	$T = 1/f$ $T = 1/4 \text{ Hz}$ $T = 0.25 \text{ sec}$

Ex: A wheel has a period of 2 seconds. Find its frequency.	
$T = 2 \text{ sec}$ $f = ?$	$f = 1/T$ $f = 1/2 \text{ sec}$ $f = 0.5 \text{ Hz}$

**Amplitude:** the maximum distance or angle the motion moves from its center position. Can be measured in distance (meters, centimeters) or degrees.



**Amplitude = 1/2(high - low)**

## Graphing Harmonic Motion

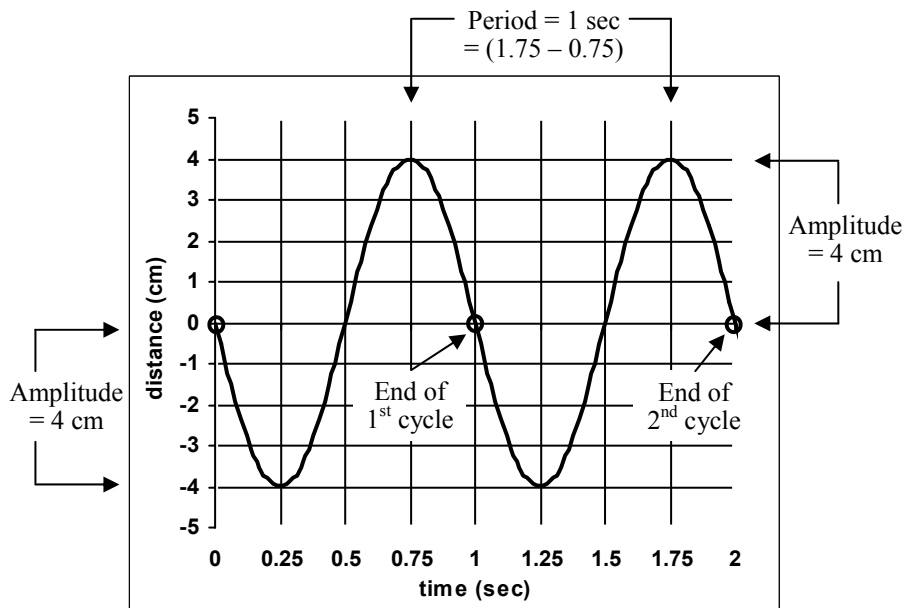
On a graph you can see all parts of harmonic motion.

**Cycle**—one repetition of the motion (top to top, bottom to bottom, etc.).

**Period**—time for one cycle; time from top to top, etc.

**Frequency**—how many cycles in one second.

**Amplitude**—how far the graph goes away from the center (or use the equation: Amplitude = 1/2(high - low))

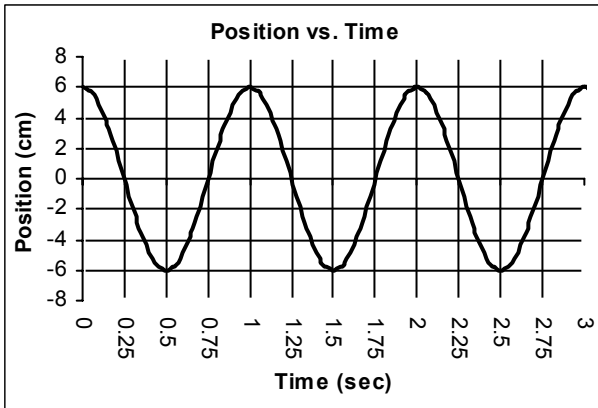


Name: \_\_\_\_\_

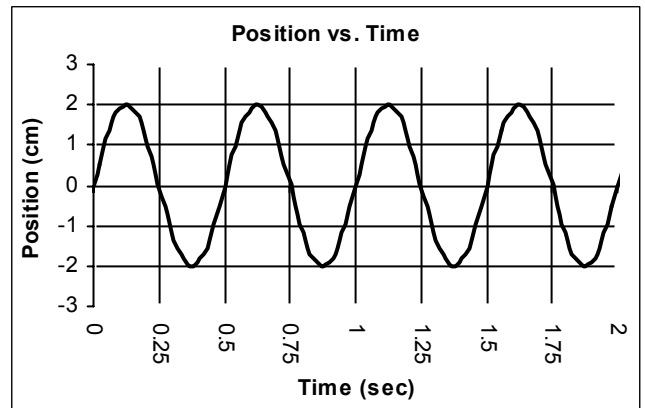
Period: \_\_\_\_\_

Harmonic (H) or Linear (L) motion?			1. Period	A. The number of cycles per second.
Person running: _____	A swing: _____	Music: _____	2. Amplitude	B. A unit of one cycle per second.
The moon: _____	A car moving: _____	Bird flying: _____	3. Frequency	C. The size or strength of a cycle.
Clock pendulum: _____	Jumping Jacks: _____	Bouncing spring: _____	4. Cycle	D. Time it takes to complete one cycle.
Ocean waves: _____	Moving bicycle: _____	A radio wave: _____	5. Hertz	E. A part of motion that repeats over and over with a set series of events.

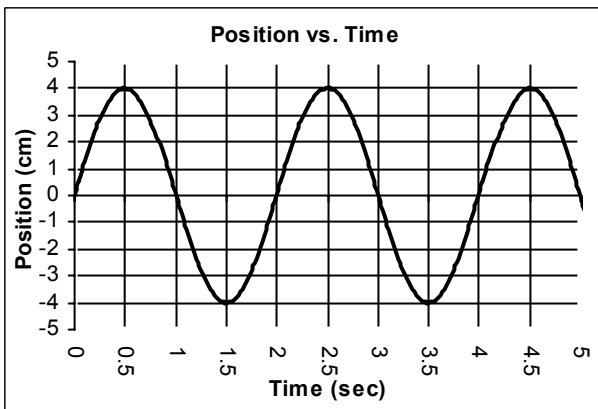
Convert from period (T) to frequency (f):		Convert from frequency (f) to period (T):	
1 sec = _____	4 sec = _____	1 Hz = _____	10 Hz = _____
0.1 sec = _____	2 sec = _____	2 Hz = _____	5 Hz = _____
0.5 sec = _____	0.25 sec = _____	0.5 Hz = _____	0.1 Hz = _____



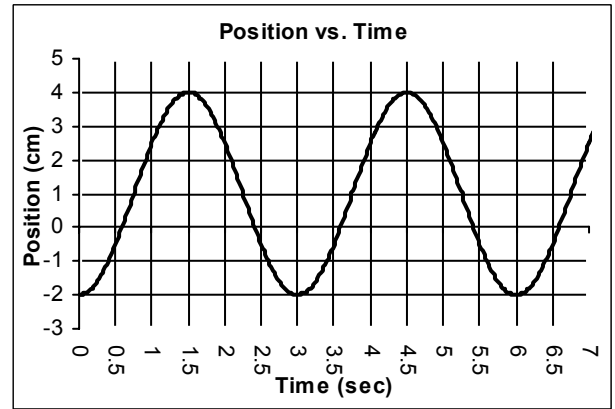
Mark 1 cycle of the harmonic motion.  
 Starting at 0 secs, when does the 1st cycle end:  
 Number of complete cycles:  
 Period: \_\_\_\_\_ Frequency: \_\_\_\_\_  
 Amplitude: \_\_\_\_\_



Mark 1 cycle of the harmonic motion.  
 Starting at 0.25 secs, when does the 2nd cycle end:  
 Number of complete cycles:  
 Period: \_\_\_\_\_ Frequency: \_\_\_\_\_  
 Amplitude: \_\_\_\_\_



Mark 1 cycle of the harmonic motion.  
 Starting at 1 secs, when does the 1st cycle end:  
 Number of complete cycles:  
 Period: \_\_\_\_\_ Frequency: \_\_\_\_\_  
 Amplitude: \_\_\_\_\_



Mark 1 cycle of the harmonic motion.  
 Starting at 0 secs, when does the 1st cycle end:  
 Number of complete cycles:  
 Period: \_\_\_\_\_ Frequency: \_\_\_\_\_  
 Amplitude: \_\_\_\_\_